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 $\frac{9}{2}$ 0 1 $\frac{1}{2}$ $\frac{1}{2$ \int_{10}^{9} S[a](#page-0-0)ndeep Khanna a,*, Suman Kundu [b](#page-0-2) and Chiranjoy Chattopadhyay [c](#page-0-3) \int_{10}^{9}

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18 **Abstract.** This paper introduces INDoRI (Indian Dataset of Recipes and Ingredients) dataset comprising of rich collection of 18 19 19 comprising of ten worldwide cuisines and constructed its Ingredient Network (InN). Further, an empirical investigation was ²⁰ performed on these multi-cuisine InN's, uncovering resemblances to social networks. The research reveals that the distribution²⁰ 21 of InN follows a power-law distribution, with an alpha exponent ranging from $\gamma = 1.96$ to $\gamma = 2.38$. This suggests that InN 21 exhibits an ultra-small world characteristic, further supported by a network diameter of 4. These measurements indicate that 22 recipes and ingredients from 18 cuisine within the Indian subcontinent. Additionally we examined two recipe ingredient datasets the InN, similar to numerous social networks, exhibits scale-free characteristics indicative of social behaviour patterns.

23 \sim 23 24 24 Keywords: Social Network Analysis, Ingredient Network, Power Law, Social Network metrics, Community structure

28 **1. Introduction** 28

³⁰ A social network can be represented as a graph consisting of individuals or entities, their intercon-³⁰ 31 nections, and the modes of communication between them [\[32,](#page-16-0) [65\]](#page-17-0). Social network analysis (SNA) is a 31 ³² method used to examine and study the different aspects and characteristics of social networks [\[51,](#page-16-1) [81\]](#page-17-1). ³² 33 SNA helps in understanding the interdependence of social entities, characterizing their activities and ³³ ³⁴ their impact on the network.³⁴

³⁵ 35 However, social networks do not have the homogeneous distribution of degrees that random networks³⁵ ³⁶ possess. A random network is constructed by placing an edge between a pair of vertices with probabil-³⁶ $\frac{37}{10}$ ity *p*, and each node's expected number of connections is equal. On the contrary, social networks are $\frac{37}{10}$ $\frac{38}{10}$ real-world networks with a few highly connected nodes and many less connected nodes. These networks ³⁹ show power-law degree distribution and are called scale-free. A scale-free network recognizes that net-³⁹ work structure and its evolution are inextricably linked [\[8\]](#page-15-0), i.e., the power law distribution results from $\frac{40}{100}$ 41 growth and preferential attachment (PA). PA says that the more connected a node is, the more likely it 42 $\frac{1}{2}$ $\frac{1}{2}$ is to receive new links. One essential characteristic of scale-free networks is their propensity to form $\frac{43}{43}$ 44 44 communities.

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21 21 Fig. 1. Random Network vs Scale Free Network 22 \sim 22

23 23 Fig [1](#page-1-0) shows a random network and a scale-free network side by side. The degree distribution for ²⁴ random networks follows Poison distribution, whereas scale-free networks offer power law. Another ²⁴ ²⁵ property of scale-free networks is that they contain hub nodes. In Fig. [1,](#page-1-0) the hub nodes are the nodes that ²⁵ ²⁶ have more connections than the average and are shown in yellow. As a result, many nodes are sparsely ²⁶ ²⁷ connected, whereas hubs can have many links. Another essential feature of a scale-free network is that ²⁷ ²⁸ the clustering coefficient drops with node degree, with progressively lower-degree nodes forming the ²⁸ 29 29 regions between the core and the periphery.

³⁰ This paper introduces the Indian Dataset of Recipes and Ingredients (INDoRI), encompassing a total ³⁰ ³¹ of 5187 recipes. Recipes were extracted and gathered from multiple online platforms [\[5,](#page-15-1) [25,](#page-16-2) [31,](#page-16-3) [35,](#page-16-4) ³¹ ³² [43,](#page-16-5) [77\]](#page-17-2). These recipes span a variety of Indian cuisines, reflecting the rich cultural diversity across ³² ³³ regions such as Punjabi, Bengali, and Gujarati. INDoRI stands as a structured repository of recipes and³³ ³⁴ their corresponding ingredients. Further, the dataset includes a graph-based representation of ingredient³⁴ ³⁵ relationships, namely, ingredient network (InN). InN is formed by capturing ingredient relationships³⁵ 36 based on their co-occurrence within recipes. Ingredient Network (InN) is essentially a graph $G(V, E, w)$ ³⁶ of ingredients [66], constructed by joining ingredients that appear together in different recipes. The ³⁷ of ingredients [\[66\]](#page-17-3), constructed by joining ingredients that appear together in different recipes. The ³⁷ ³⁸ vertices *V* represent the ingredients, edges *E* contain the connection between vertices, and the weight ³⁸ ³⁹ *w* represents the strength of the association. The association is stronger if ingredients appear multiple ³⁹ ⁴⁰ times in different recipes. For example, the ingredients 'onion' and 'tomato' have a strong association as ⁴⁰ ⁴¹ they seem numerous times in many recipes (refer Fig. [3\)](#page-5-0). The dataset and its characteristics were earlier ⁴¹ ⁴² published in [\[45\]](#page-16-6). Extended research involves studying the dataset property and comparison with other ⁴² ⁴³ cuisine through detailed empirical analysis. This work is mostly emphasized in this paper. ⁴³

⁴⁴ Any study on a novel network starts with empirical analysis to know whether the network is generated ⁴⁴ ⁴⁵ randomly or through preferential attachment. In the same sense, it is interesting to know the character-⁴⁵ 46 46 1 istics of InN. The heterogeneous degree distribution in ingredient networks becomes evident as certain 1 2 ingredients are essential in numerous recipes while others are only present in a few dishes. This obser- 3 vation highlights the varying degrees of ingredient usage, emphasizing each ingredient's diverse role 4 within the network. However, *are these differences in degree significant enough to call this network* 5 *a social network? Does the degree of this network a power law distribution?*. In this paper, we have 6 addressed these questions through an extensive empirical analysis.

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$8 \t 8$ $\frac{9}{9}$ 2. Related to the set of $\frac{9}{9}$ 2. Related Work

¹⁰ The theory of complex networks characterizes social networks by a scale-free property [\[9\]](#page-15-2). This prop-¹¹ erty allows it to pose specific properties different from the random network. Although the study of social¹¹ ¹² network analysis started with the human relational network [\[58\]](#page-17-4), researchers have investigated and ex-¹² ¹³ plored various other networks and found that many are structurally similar to social networks [\[89\]](#page-18-0). The ¹³ ¹⁴ original attempt of Watts and Strogatz in their work on small-world networks [\[91\]](#page-18-1) was to construct a¹⁴ ¹⁵ network model with a small average path length as a random graph and a relatively large clustering coef-¹⁵ ¹⁶ ficient as a regular lattice, which evolved to become a new network model as it stands today. On the other ¹⁷ hand, the discovery of scale-free networks was based on the observation that the degree distributions of ¹⁷ ¹⁸ many real networks have a power-law form, albeit power-law distributions. Another significant recent¹⁸ ¹⁹ discovery is that many large-scale complex networks are scale-free; that is, their connectivity distribu-¹⁹ ²⁰ tions are in a power-law form independent of the network scale [\[8,](#page-15-0) [10\]](#page-15-3). Unlike an exponential network, ²⁰ ²¹ a scale-free network is homogeneous: most nodes have very few link connections, yet few nodes have ²¹ 22 monu connections 22 many connections.

23 23 Social Network Analysis (SNA) has been applied to various networks, with some of the notable ex-²⁴ amples being Twitter [\[18,](#page-15-4) [56,](#page-17-5) [100\]](#page-18-2), Facebook [\[19,](#page-15-5) 100], human interaction networks [\[20\]](#page-15-6), Internet [\[86\]](#page-18-3), ²⁴ ²⁵ WWW [\[1\]](#page-15-7), E-mail [\[28\]](#page-16-7), software [\[85\]](#page-18-4), electronic circuits [\[39\]](#page-16-8), language [\[17\]](#page-15-8), movie actors [\[8,](#page-15-0) [91\]](#page-18-1), math ²⁵ ²⁶ coauthorship [\[62\]](#page-17-6), food web [\[57,](#page-17-7) [93\]](#page-18-5), metabolism [\[40\]](#page-16-9) where these networks were analyzed and proved²⁶ ²⁷ that they all follow the small world pattern and are scale-free. In contrast, the analysis of the biomedical 27 ²⁸ research collaboration network [\[12\]](#page-15-9) shows that the collaboration networks are not scale-free but have ²⁸ ²⁹ small-world properties. Similarly, the Power Grid network is also not scale-free [\[68\]](#page-17-8). Researchers have ²⁹ ³⁰ investigated ingredient networks within different contexts, including identification of communities [\[82\]](#page-17-9), ³⁰ ³¹ recipe recommendation [\[66\]](#page-17-3), and recipe recognition [\[55\]](#page-17-10). However, none of these studies investigate³¹ 32 32 whether InN shows randomness or scale-free characteristics. 33 33

35 35 3. Methodology

 36 37 The overall pipeline is structured into several key stages: initially introducing the dataset, followed by 37 ₃₈ cleaning it and constructing an Ingredient Network (InN). Subsequently, the focus shifts to analyzing ₃₈ 39 various cuisines through social network metrics. Additionally, the investigation explores the communi- $_{40}$ ties within the InN, comparing these findings across different community detection algorithms. These $_{40}$ ⁴¹ steps are elaborated in the subsequent Sections.⁴¹

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$\frac{42}{11}$ $\frac{11}{11}$ $\frac{1$ 43 43 *3.1. INDoRI*

⁴⁴ Creating a comprehensive dataset of Indian cuisines possesses unique challenges. One of them is to ⁴⁴ ⁴⁵ compiling recipes that span diverse cultural landscape of India. Due to the same reason one may not ⁴⁵ 46 46

 23 $_{24}$ find all the recipes from one single web portal. As there is no common data format available, each $_{24}$ ₂₅ portal present data differently and the data are unstructured. Hence the second challenge is to extract ₂₅ ₂₆ meaningful information from it. We consider multiple recipe websites to address the first challenge. All ₂₆ 27 the unstructured data therein are crawled using Python script. 27 27

 \sim 22

 28 INDoRI encompasses 5,187 recipes representing 18 diverse Indian cuisines. Additionally it encom- 29 passes additional attributes such as cuisine, category, and preparation time. All recipes are classified into 30 8 different types. Apart from 925 unclassified recipes rest are also categorized into 18 different cuisines 31 Fig. [2](#page-3-0) shows the key characteristics of INDoRI.

³² Detailed information about the INDoRI dataset, the cleaning process and ingredient stop words can³² be found in [\[45\]](#page-16-6). 33 34

35 35 $\frac{36}{36}$ $\frac{3$ *3.2. Dataset for Empirical Analysis*

 37 38 We utilized two datasets to create, analyze, and understand ingredient networks. The first dataset, 38 39 INDoRI, is a comprehensive compilation of Indian recipes and their corresponding ingredients.

 40 In addition to the INDoRI dataset, we incorporated the recipe ingredient dataset sourced from Yummly ⁴¹ [\[99\]](#page-18-6). This dataset contains ingredient information from over 14 global cuisines. For our analysis, we ⁴¹ ⁴² deliberately selected and filtered nine cuisines based on their popularity and the quantity of available ⁴² ⁴³ records. In summary, our study focuses on analysing ingredient networks from 10 cuisines. Table [1,](#page-4-0) you ⁴³ ⁴⁴ can observe the distribution of recipes for each cuisine. Notably, Italian and Mexican cuisines have the ⁴⁴ ⁴⁵ highest number of recipes, followed closely by Indian cuisine. ⁴⁵ 46

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Table 2 Sample Ingredient Stop Words. drops sunflower kept florets adding handful chopped colostrum shah consistency karhai take strips sabut handful ones cup magaz tightly pass sprig strong must to boiling kootu quick purpose seedless pieces substitute more pour dounces inches mix quality inches approx equired Kg | grain | drop | outer | sprigs fat crumbled out lengthwise each

15 15 *3.3. Data Cleaning*

¹⁷ The datasets we used contain extraneous details beyond just ingredient names, necessitating the re-¹⁷ ¹⁸ moval of certain words like "kg," "gms," "cup," "tbls," "pinch," "chopped," "boiled," "sliced," and ¹⁸ ¹⁹ "split" to refine our data. These words, categorized as Ingredient Stop Words (ISW), are sourced from ¹⁹ ²⁰ [\[45\]](#page-16-6) and include a total of 527 such terms. For instance, the phrase "half cup of sugar" includes un-²¹ necessary descriptors; by applying ISW filters, we simplify it to just "sugar." This process of removing ²¹ ²² ISWs ensures that our Ingredient Network (InN) is constructed with only the essential ingredient names, ²² ²³ leading to a cleaner and more accurate dataset. For reference, examples of such words can be found in²³ 24 the referenced Table [2.](#page-4-1) 24

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29 29 $\frac{\text{Rathal}}{30}$ $\frac{\text{Rathal}}{30}$ $\frac{\text{Rathal}}{30}$ $\frac{\text{Rathal}}{30}$ $\frac{\text{Rathal}}{30}$ $\frac{31}{2}$ $\frac{1}{2}$ 32 $\frac{1}{2}$ 32

 $\frac{1}{2}$ 33 $\frac{34}{2}$ $\frac{34}{2}$

$\frac{1}{1}$ $\frac{1}{2}$ $\frac{1}{2}$

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За применение село в село 38 38

39 39 *3.4. Ingredient Network (InN) Construction*

⁴¹
We developed an ingredient network, represented as a graph $G(V, E, w)$, where *V* is a set of ingredients,
⁴²
F is the connections between ingredients and $w : V \times V \rightarrow R$ of an edge signifies the number of ⁴² E is the connections between ingredients and $w : V \times V \to R$ of an edge signifies the number of ⁴² ⁴³ association between ingredients in different recipes. Here each node corresponds to an ingredient and an ⁴³ ⁴⁴ edge is formed between two nodes if the corresponding ingredients appear together in the same recipe. ⁴⁴ ⁴⁵ The more they appear together in diverse recipes, the stronger the association. A visual representation ⁴⁵ 46 46

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29 30 30 *3.5. Social Metrics Evaluation*

 $\frac{31}{22}$ In order to examine the dynamics and behaviour of InN, we utilised a range of social network mea- $\frac{32}{22}$ surements, which we classified into macro and micro metrics. Macro metrics, such as distance, diameter, $\frac{33}{24}$ and density, provide valuable information about the insights of the network. On the other hand micro 34 and density, provide valuable information about the morgins of the new only on the state name into 34 metrics, such as node degree, cluster coefficient, proximity centrality, and eigencentrality, provide a $\frac{35}{35}$ 36 36 obtained from these metrics are explained in the Results Section, demonstrating how each statistic adds $\frac{37}{37}$ to a thorough comprehension of the InN features. detailed perspective by assessing the behaviour of individual components in the network. The results

39 39 *3.6. Community Structure Identification* 40 40

⁴¹ Scale-free networks exhibits community structure. In the course of studying and analyzing InN, we ⁴¹ ⁴² also tried to identify communities within InN. We employed diverse community detection algorithms ⁴² ⁴³ to partition the InN into multiple communities. Specifically, we implemented weighted versions of the ⁴³ ⁴⁴ Leiden [\[83\]](#page-17-11), Louvain [\[13\]](#page-15-10), and Weighted Association Based Community Detection (WABCD) [\[45\]](#page-16-6) al-⁴⁴ ⁴⁵ gorithms. It was observed that InN too exhibits community structure like other scale-free networks. ⁴⁵ 46 46

1 1 Notably, the weighted Louvain and Leiden algorithms organized communities based on a weighted mod-2 2 ularity score, while the WABCD method grouped ingredients by the strength of their connections. The 3 3 details of these community structures and their implications are further discussed in the Results Section.

ϵ 4. Results ϵ 4. Results

8 8 This section provides an in-depth analysis of the outcomes of different macroscopic and microscopic ⁹ measurements of social networks, along with the observed trends within communities. The subsequent ⁹ ¹⁰ Discussion Section further explores and elaborates on the implications of these metrics.¹⁰

12 12 *4.1. Degree Distribution of InN*

¹⁴ The degree distribution of the Ingredient Network (InN) for ten different cuisines adheres closely to a ¹⁴ ¹⁵ power law, as demonstrated by our analysis. We modeled this behavior using a power law distribution, ¹⁵ ¹⁶ detailed in Equation [1,](#page-6-0) and visually represented the fit with a red line in Fig. [4](#page-7-0) and Fig. [5.](#page-8-0) Notably, the ¹⁶ ¹⁷ parameter γ varies among the cuisines, ranging from 1.96 in Italian Cuisine to 2.38 in Indian Cuisine, ¹⁷
¹⁸ bigblighting the distinct ingredient combinations characteristic of each cuisine ¹⁸ highlighting the distinct ingredient combinations characteristic of each cuisine.¹⁸ 19 19

$$
p_k \sim k^{-\gamma} \tag{1} \qquad \qquad p_k \sim k^{-\gamma} \tag{2}
$$

23 and $\frac{1}{2}$ 23 24 24 24 *4.2. Distance*

 25 25 26 In graph theory, the distance between two vertices is defined as the number of edges in the shortest 26 $_{27}$ path connecting them, often referred to as the hop distance. This concept is mathematically expressed $_{27}$ 28 **as.** 28 as:

$$
d(V_i, V_j) = \min \text{hopdistance}(V_i, V_j) \tag{2}
$$

33 where $d(V_i, V_j)$ represents the minimum number of hops between vertex V_i and vertex V_j . In the 33
34 context of the Ingredient Network (InN) this distance can reveal how closely two ingredients are related 34 context of the Ingredient Network (InN), this distance can reveal how closely two ingredients are related 35 in terms of their use in recipes. A shorter distance between two ingredients suggests they frequently 36 appear together in recipes, indicating a strong culinary link.

37 37 Our analysis of different cuisines revealed varying maximum distances, underscoring the ultra-small-38 world nature of these networks. For instance, the maximum distance in the InN of Indian cuisine is 4, ³⁸ ³⁹ indicating a broader variety of ingredient pairings, whereas in Thai cuisine, the maximum distance is ³⁹ ⁴⁰ only 2, suggesting a tighter integration of ingredients. Other cuisines typically exhibited a maximum ⁴⁰ ⁴¹ distance of 3, further demonstrating the close-knit structure of these culinary networks. ⁴¹

43 43 *4.3. Diameter*

⁴⁵ The diameter of a graph is determined by its maximum eccentricity, which is calculated as follows: 46 46

Fig. 4. Degree Distribution Comparison of 6 Cuisine's Ingredient Network along with fitted power law.

⁴² In these equations, $E(V_i)$ represents the eccentricity of vertex V_i , defined as the greatest distance ⁴² ⁴³ from V_i to any other vertex V_j . The graph's diameter, $D(G)$, is then the largest eccentricity among all ⁴³ ⁴⁴ vertices in the graph. This metric reflects the farthest distance between any two nodes in the network. ⁴⁴ ⁴⁵ Notably, in the Ingredient Network (InN) for each cuisine analyzed, the diameter consistently measures ⁴⁵ 46

4 4

1 1 4. This uniformity across different cuisines suggests that, regardless of the specific ingredients involved, 2 any ingredient can be connected to any other through no more than four steps, illustrating the closely 2 3 3 interconnected nature of culinary ingredients within these networks.

 $\frac{4.4.}{5}$ $\frac{9}{5}$ $\frac{4.4.}{5}$ Density *4.4. Density*

 6 $_{7}$ Density in a network measures the proportion of actual edges to the maximum possible edges between $_{7}$ $8₈$ nodes, reflecting the network's connectivity. The denser a network, the more interconnected it is, with $8₈$ a high number of edges relative to the number of nodes. The density of the Ingredient Network (InN) $\frac{1}{9}$ varies across different cuisines, with node counts ranging from 784 in British cuisine to 1926 in Italian $_{10}$ cuisine, and edge counts from 14479 to 62528, respectively. Density is calculated as follows:

 12 and 12

$$
Density = \frac{\text{Actual number of Edges}}{\text{Maximum possible edges}} \tag{5}
$$

¹⁶ where the maximum possible edges for a graph with *n* nodes is $\binom{n}{2}$. In our analysis, the density values ¹⁷ for InN across cuisines ranged from 0.0296 for Indian cuisine to 0.067 for Thai cuisine. These values in- 18 dicate that the ingredient relationships in the InN for each cuisine are relatively sparse, as densities close 18 ¹⁹ to 0 suggest a network with few connections relative to the number of possible connections, whereas ¹⁹ 20 20 densities near 1 indicate a highly interconnected network. 21 21 $n \choose 2$. In our analysis, the density values

22 22 *4.5. Cluster Coefficient*

24 24 The clustering coefficient is an essential metric in social network analysis as it indicates the degree to 25 25 which nodes tend to cluster together, reflecting community formation and shared interests, as highlighted 26 26 by Katzir et al. [\[44\]](#page-16-10). Applied to the Ingredient Network (InN), this coefficient can identify groups of ²⁷ ingredients that are commonly used together in specific types of recipes. The formula for calculating the ²⁷ 28 clustering coefficient for a node *i*, which has n_i neighbors, is: 28

 29

 23 23

$$
C_i = \frac{2e_i}{n_i(n_i - 1)}
$$

33 33 Here, C_i represents the clustering coefficient for node *i*, where e_i is the number of actual connections $\frac{34}{34}$ between the node's n_i neighbors. The value of C_i is essentially the proportion of these connections $\frac{35}{35}$ 36 CHARLO to the total possible connections among the neighbor. In Sea analysis of the HIV, the average clustering coefficients vary significantly across cuisines, from 0.7986 in French cuisine to 0.8399 in $\frac{37}{37}$ Mexican cuisine, indicating a strong tendency for ingredients within these cuisines to be interconnected $\frac{38}{38}$ $\frac{39}{39}$ $\frac{39}{39}$ $\frac{39}{39}$ $\frac{39}{39}$ relative to the total possible connections among the neighbors. In our analysis of the InN, the average within recipes.

40 40 *4.6. Closeness Centrality* 41 41

⁴² Closeness Centrality (CC) is a critical measure for understanding the proximity of vertices in a graph, ⁴² ⁴³ which in the context of the Ingredient Network (InN), helps identify how readily accessible ingredients⁴³ ⁴⁴ are to each other and reveals the flexibility in ingredient usage across recipes. CC is calculated using the ⁴⁴ $\frac{45}{45}$ formula: $\frac{45}{45}$ 46 46 formula:

$$
C(V_i) = \sum_{V \in G} \frac{1}{d(V_i, V_j)}
$$
\n(7) 23
\n 24
\n 25
\n(8) 24
\n 25
\n(9) 24
\n 25

22 \sim 22

 26 26 A histogram illustrating the CC values for all ingredients is presented in Fig. [6,](#page-10-0) highlighting the range $\frac{27}{27}$ 28 of closeness centrality, which typically spans from 0.4 to 0.6 for every cuisine in the InN. This range 28 29 29 indicates the degree of closeness and connectivity among ingredients within the various cuisines.

 30 7π π π $\frac{31}{31}$ \cdots $\frac{25}{31}$ \cdots $\frac{31}{31}$ *4.7. Eigen Centrality*

³² Eigen centrality (EC) is a key metric for determining the importance of nodes within a network, as it quantifies the influence of a node based on its connections to other highly significant nodes, as outlined ³⁴ by South et al. [\[80\]](#page-17-12). In the context of the Ingredient Network (InN), EC has been applied to assess ³⁴ $\frac{35}{25}$ the significance of each ingredient. It has been found that the EC values for most ingredients in every ³⁶ cuisine generally fall between 0.01 and 0.08. However, as depicted in Fig. [7,](#page-11-0) there are a few ingredients that stand out with notably higher EC values, underscoring their pivotal roles within their respective 37 $\frac{37}{100}$ denotes the stable higher EG also and see the second extended with the second $\frac{37}{100}$ that stand out with notably higher EC values, underscoring their pivotal roles within their respective $\frac{38}{38}$ 39 39 culinary networks.

⁴² The Ingredient Network (InN) was analyzed using the Weighted Leiden (W-Leiden), Louvain (W-
⁴² ⁴³ Louvain), and WABCD algorithms [\[45\]](#page-16-6), to identify distinct culinary communities within various⁴³ ⁴⁴ cuisines. The results from the W-Leiden algorithm revealed that the number of communities ranged ⁴⁴ ⁴⁵ from 3 in Italian cuisine to 8 in Japanese cuisine. In contrast, the W-Louvain algorithm detected between ⁴⁵ 46 46

⁴⁰ 40 *4.8. Community Structure* 41 41

20 20 Fig. 7. Eigen Centrality Distribution for the Ingredient Network.

21 $\hspace{1.5cm}$ 21 22 4 communities in several cuisines such as Chinese, Japanese, Italian, and Thai, and up to 9 in British 22 cuisine, with Southern US cuisine standing out with 17 communities. The WABCD algorithm showed a $_{23}$ variation from 6 communities in Chinese cuisine to 9 in Southern US cuisine. These findings underscore the tendency of the InN to form community structures similar to other social networks.

 $_{26}$ Fig. [8](#page-12-0) presents the community detection results within the Indian cuisine InN, illustrating the seg-27 mentation achieved by the WABCD, W-Leiden, and W-Louvain algorithms, which identified 7, 5, and 4 $_{27}$ 28 distinct communities, respectively. The figure clearly shows that the first community identified by each 28 algorithm is characterized by tightly interconnected nodes, indicating strong cohesion. However, the $_{29}$ ³⁰ density of nodes and the connectivity within communities tend to decrease in subsequent groups iden-³¹ tified by each algorithm, reflecting a varying degree of association among different ingredient groups. ³² 32 These patterns suggest underlying structures in the data that mirror complex relationships within the ³² $\frac{33}{33}$ cumary domain. culinary domain.

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35 ϵ Discussion 35 36 5. Discussion

³⁷ Results of the empirical study reveal that InN shows properties which resemble scale-free networks.³⁷ ³⁸ For example, Fig. [4](#page-7-0) and Fig. [5](#page-8-0) demonstrates that InN follows a power law degree distribution with expo-³⁸ ³⁹ arent γ = 1.96 to γ = 2.38. This value of γ ensures ultra-small property [\[23\]](#page-16-11), i.e., the average diameter ³⁹
⁴⁰ is minimal. The same is found in our experiment: the diameter value is 4. On the contrary a random ⁴⁰ is minimal. The same is found in our experiment; the diameter value is 4. On the contrary, a random 40 ⁴¹ network usually has γ ≥ 3 [\[7\]](#page-15-11). For reader's reference, the degree of separation comparison between real ⁴¹
⁴² networks and InN for Indian cuisine is shown in Table 3. The table shows the average and maximum ⁴² ⁴² networks and InN for Indian cuisine is shown in Table [3.](#page-13-0) The table shows the average and maximum⁴² ⁴³ distances of the 5 real undirected networks and InN. The columns N, L, k, d and d_max represent the ⁴³ ⁴⁴ number of nodes, links, average degree, average distance and maximum distance, respectively. In other ⁴⁴ ⁴⁵ words, d_max is the diameter. Degrees of separation specify how many hops one must reach from any ⁴⁵ 46 46

 be reached from any node through a maximum hop of 4. The average degree of separation is 3.12. This 35
corresponds to the phenomenon of six degrees of separation [27, 54, 84], which save one node can be corresponds to the phenomenon of six degrees of separation [\[27,](#page-16-12) [54,](#page-17-13) [84\]](#page-18-7), which says one node can be 36 reachable through a maximum of 6 hops [\[61\]](#page-17-14). Although theoretically, this represents the diameter as 6, 37 38 practically, the average distance stays at 6 or less. The actual diameter sometimes shows higher values 38 39 because of outliers. For all pairs of Facebook users worldwide and within the United States, the average 39 distance separation is only 3.90 [\[6\]](#page-15-12). However, there are networks like Power Grid where the average 40
distance between nodes exceeds 10 degree of separation. Most real-world social networks adhere to the ⁴¹ distance between nodes exceeds 10 degree of separation. Most real-world social networks adhere to the ⁴¹ ⁴² six degrees of separation principle. Such a network does not show power law distribution. ⁴²

⁴³ The nodes of InN adhere to an 80:20 ratio, meaning that 80 per cent of the nodes have a low degree ⁴³ ⁴⁴ and 20 per cent have a higher degree. For InN, most nodes (597) have degrees ranging from 0-100, and ⁴⁴ ⁴⁵ a smaller number of nodes (156) have degrees ranging from 200 - 500. 46

 $\frac{1}{1}$ 1 $_2$ Comparison of Real World Undirected Networks with Ingredient Network as to Degree separation and Fluctuations [\[61\]](#page-17-14). Table 3

Table [4](#page-13-1) compares ingredient networks for ten cuisines. It is noteworthy that the InN exhibits similar 15 characteristics for most cuisines. These networks' distance and diameter metrics are consistently around $\frac{16}{16}$ 3 and 4, respectively, indicating an ultra-small world property. Additionally, the degree distribution met-
17 ric varies from 1.96 (Italian cuisine) to 2.38 (Indian cuisine), indicating a scale-free network property. This suggests that some ingredients have many connections in these networks, while most have fewer 20 connections, contributing to a search contribution. connections, contributing to a scale-free structure.

21 21 Furthermore, the density metric, which reflects the level of connectivity within the InNs, ranges from 22 0.033 (for Italian and Southern US cuisines) to 0.067 (for Thai cuisine). This metric further supports the 22 scale-free nature of these networks, as it indicates that specific nodes have a high degree of connections ₂₃ while the majority have fewer connections.

25 A particularly intriguing observation is that these InNs tend to form communities, with the number 25 $_{26}$ of communities ranging from 3 to 9. These communities were identified through weighted Louvain, weighted Leiden, and WABCD. The only exception to this pattern is the InN for Southern US cuisine, $_{27}$ 28 where weighted Leiden identifies more communities, precisely 17.

Table 4

⁴¹ Fig [4](#page-7-0) shows the degree distribution of InN for ten cuisines. It is evident that the degree distribution for ⁴¹ ⁴² each InN closely adheres to a power law, with the degree distribution curves nearly aligning along the ⁴² 43 43 central diagonal line.

40 40

For a random network, the standard deviation follows $SD = \langle k \rangle 1/2$ as shown in Fig. [9,](#page-14-0) which depicts 44
⁴⁵ SD for 4 out of 5 reference networks calculated using Table 3 plus InN. The actor network has a very ⁴⁵ 45 SD for 4 out of 5 reference networks calculated using Table [3](#page-13-0) plus InN. The actor network has a very 45 46 46

¹⁶ Fig. 9. An illustration of the comparison of standard deviation in Real World Networks with Ingredient Network. 17 17

¹⁸ 18 1arge $\langle k \rangle$ and SD; hence it is omitted for clarity. Each network's SD is more significant than predicted for ¹⁹ a random network of the same $\langle k \rangle$. The power grid is the only exception, which is not scale-free. With ¹⁹ ²⁰ its small standard deviation, InN is effectively scale-free. ²⁰

²¹ 21 The InN was also tested on other social network metrics and was discovered to behave similarly to ²¹ ²² most real-world social networks. Both macroscopic and microscopic metrics were calculated on InN. ²² ²³ Distance metric shown in Section [4.2](#page-6-1) is computed to identify the reachability of one node to the other.²³ ²⁴ Most nodes can be visited from any node in a maximum hop of 3, whereas some require 4 hops. Most ²⁴ ²⁵ real-world social networks follow this property. The density metric is calculated for the InN shown in²⁵ ²⁶ Section [4.4,](#page-9-0) and it has been found that InN has sparse connections, similar to most real-world social²⁶ networks. The average clustering coefficient of InN is calculated, shown in Section [4.5,](#page-9-1) to be 0.8176, 27
²⁸ indicating the formation of a cluster where maximum nodes tend to form a more extensive cluster. The ²⁸ indicating the formation of a cluster where maximum nodes tend to form a more extensive cluster. The ²⁸ ²⁹ majority of real-world social networks follow this property. Another metric, closeness centrality, shown²⁹ ³⁰ in Section [4.6](#page-9-2) is also calculated for InN, which verifies that the new addition of nodes to the graph is³⁰ ³¹ more likely to connect with the existing popular ones. Eigen centrality shown in Section [4.7](#page-10-1) for InN³¹ ³² indicates that few nodes had high connections, with most popular ones resembling the same behaviour³² ³³ as a social network. These calculated graph metrics also added weightage to the conclusion that InN³³ ³⁴ mimics social behaviour and property. A summary of the computed social metrics on InN is shown in³⁴ $\frac{35}{11}$ $\frac{7}{11}$ $\frac{35}{11}$ $\frac{35$ 36 Table [4.](#page-13-1)

37 37

38 6. Conclusion and Future Work 38 39 39

⁴⁰ In this paper, we conducted an empirical study to demonstrate that a network of food ingredients (InN), ⁴⁰ ⁴¹ like any other social network, manifests social behaviour. We carried out a thorough examination and the ⁴¹ ⁴² computation of pertinent metrics. The study revealed that InNs follow a power law, a defining feature of ⁴² ⁴³ a scale-free network. We have discussed various social network metrics and community detection results ⁴³ ⁴⁴ on InN. We have conducted experiments on ten types of cuisines and evaluation metrics across different ⁴⁴ 45 45 cuisines that conform to social network-like behaviour.46 46 *S.K. Khanna et al. / Are Food Ingredient Social? An Empirical Investigation*

 1 In food computing, future research can analyse user interactions within cuisine networks to understand 2 cultural nuances and culinary evolution. Future work paves the way for developing advanced algorithms 3 and models for predicting culinary trends and fostering cross-cultural culinary exchanges within these 4 networks. Additionally, our findings serve as a stepping stone for prospective research endeavours that 5 focus on the ever-evolving impact of social networks on the dynamic landscape of food computing. 7 8 8 8 **Declaration of Conflicting Interests** en de la construction de la constr
De la construction de la construct 10 10 10 10 The author(s) declared no potential conflicts of interest with respect to the research, authorship, and/or $_{11}$ publication of this article. and 12 13 14 15 16 The dataset used in this study is available online at<https://figshare.com/s/12a1bce0210a7f031168> 17 $\frac{18}{18}$ 18 $\frac{19}{19}$ 19 20 [1] R. Albert, H. Jeong and A.-L. Barabási, Diameter of the world-wide web, *nature* 401(6749) (1999), 130–131. 21 [2] C.L. Apicella, F.W. Marlowe, J.H. Fowler and N.A. Christakis, Social networks and cooperation in hunter-gatherers, 22 *Nature* 481(7382) (2012), 497–501. 23 [3] S. Aslan and M. Kaya, Link prediction methods in bipartite networks, in: *2017 International Conference on Computer* ²⁴ [4] L. Atzori, A. Iera, G. Morabito and M. Nitti, The social internet of things (siot)–when social networks meet the internet ²⁴ 25 of things: Concept, architecture and network characterization, *Computer networks* 56(16) (2012), 3594–3608. $_{26}$ [5] V. Azmanov, EAST INDIAN RECIPES,<https://eastindianrecipes.net> [accessed May 6, 2021].. 27 [6] L. Backstrom, P. Boldi, M. Rosa, J. Ugander and S. Vigna, Four degrees of separation, in: *Proceedings of the 4th Annual* 28 [7] A.-L. Barabási, Network science book, *Network Science* 625 (2014). 29 [8] A.-L. Barabási and R. Albert, Emergence of scaling in random networks, *science* 286(5439) (1999), 509–512. 30 [9] A.-L. Barabási and E. Bonabeau, Scale-free networks, *Scientific american* 288(5) (2003), 60–69. 31 *chanics and its Applications* 272(1–2) (1999), 173–187. 32 [11] J.A. Barnes, Class and committees in a Norwegian island parish, *Human relations* 7(1) (1954), 39–58. $_{33}$ [12] J. Bian, M. Xie, U. Topaloglu, T. Hudson, H. Eswaran and W. Hogan, Social network analysis of biomedical research $_{33}$ 34 [13] V.D. Blondel, J.-L. Guillaume, R. Lambiotte and E. Lefebvre, Fast unfolding of communities in large networks, *Journal* 35 *of statistical mechanics: theory and experiment* 2008(10) (2008), P10008. 36 [14] C. Böde, I.A. Kovács, M.S. Szalay, R. Palotai, T. Korcsmáros and P. Csermely, Network analysis of protein dynamics, 37 [15] A.D. Broido and A. Clauset, Scale-free networks are rare, *Nature communications* 10(1) (2019), 1–10. 38 [16] U. Can and B. Alatas, A new direction in social network analysis: Online social network analysis problems and applica- 39 tions, *Physica A: Statistical Mechanics and its Applications* 535 (2019), 122372. 40 [17] R.F.I. Cancho and R.V. Solé, The small world of human language, *Proceedings of the Royal Society of London. Series* 41 **41 EXECUTE:** B. Blook and C. Schifanella, Emerging topic detection on twitter based on temporal and social terms ⁴¹ 42 evaluation, in: *Proceedings of the tenth international workshop on multimedia data mining*, 2010, pp. 1–10. 43 [19] V. Chandola, A. Banerjee and V. Kumar, Anomaly detection: A survey, *ACM computing surveys (CSUR)* 41(3) (2009), ⁴⁴ $^{1-36}$. [20] Y. Cho, J. Hwang and D. Lee, Identification of effective opinion leaders in the diffusion of technological innovation: A 45 social network approach, *Technological Forecasting and Social Change* 79(1) (2012), 97–106. 46 INDoRI References *Science and Engineering (UBMK)*, IEEE, 2017, pp. 1095–1099. *ACM Web Science Conference*, 2012, pp. 33–42. [10] A.-L. Barabási, R. Albert and H. Jeong, Mean-field theory for scale-free random networks, *Physica A: Statistical Me*collaboration networks in a CTSA institution, *Journal of biomedical informatics* 52 (2014), 130–140. *FEBS letters* 581(15) (2007), 2776–2782. *B: Biological Sciences* 268(1482) (2001), 2261–2265. 1–58.

- 1 1 [21] J.H. Choi, G.A. Barnett and B.-S. CHON, Comparing world city networks: a network analysis of Internet backbone and 2 2 air transport intercity linkages, *Global Networks* 6(1) (2006), 81–99.
- [22] M. Ciba, Synchrony Measurement and Connectivity Estimation of Parallel Spike Trains from in vitro Neuronal Net-
3
3
3 works, PhD thesis, 2021. doi:10.25972/OPUS-22364.
- 4 4 [23] R. Cohen and S. Havlin, Scale-free networks are ultrasmall, *Physical review letters* 90(5) (2003), 058701.
- 5 5 [24] M. Coscia, G. Rossetti, F. Giannotti and D. Pedreschi, Uncovering hierarchical and overlapping communities with a 6 6 local-first approach, *ACM Transactions on Knowledge Discovery from Data (TKDD)* 9(1) (2014), 1–27.
- [25] Dassana, DASSANA'S VEG RECIPES,<https://www.vegrecipesofindia.com> [accessed May 7, 2021].
- 7×26 E. De Gioannis, F. Bianchi and F. Squazzoni, Gender bias in the classroom: A network study on self and peer ability 8 8 attribution, *Social Networks* 72 (2023), 44–51.
- 9 9 [27] I. de Sola Pool and M. Kochen, Contacts and influence, *Social networks* 1(1) (1978), 5–51.
- 10 10 [28] H. Ebel, L.-I. Mielsch and S. Bornholdt, Scale-free topology of e-mail networks, *Physical review E* 66(3) (2002), 035103.
- ¹¹ [29] D.A. Eisenberg, J. Park and T.P. Seager, Sociotechnical network analysis for power grid resilience in South Korea,¹¹ 12 12 *Complexity* 2017 (2017).
- 13 13 [30] D.I.H. Farías, V. Patti and P. Rosso, Irony detection in twitter: The role of affective content, *ACM Transactions on Internet Technology (TOIT)* 16(3) (2016), 1–24.
- 14

[31] I.F. Forever,<https://nerdyfoodies.com/indian-spices-list-3291.html> [accessed May 5, 2021]..
- 15 15 [32] N.A. Ghani, S. Hamid, I.A.T. Hashem and E. Ahmed, Social media big data analytics: A survey, *Computers in Human* 16 16 *Behavior* 101 (2019), 417–428.
- 17 [33] H. Ghotra,<https://www.harighotra.co.uk/indian-recipes> [accessed May 5, 2021].. 17
- 18 18 [34] M. Gong, Q. Cai, M. Lijia and L. Jiao, *Big Network Analytics Based on Nonconvex Optimization*, 2016, pp. 345–373. ISBN [978-3-319-30263-8.](http://www.isbnsearch.org/isbn/978-3-319-30263-8) doi:10.1007/⁹⁷⁸ [−] ³ [−] ³¹⁹ [−] ³⁰²⁶⁵ [−] ²15.
- ¹⁹ [35] M.F. Group., allrecipes,<https://www.allrecipes.com> [accessed May 7, 2021].
- 20 20 [36] B. Hajian and T. White, Modelling influence in a social network: Metrics and evaluation, in: *2011 IEEE Third Inter-*21 21 *national Conference on Privacy, Security, Risk and Trust and 2011 IEEE Third International Conference on Social Computing*, IEEE, 2011, pp. 497–500.
- ²² [37] C. He, X. Fei, Q. Cheng, H. Li, Z. Hu and Y. Tang, A survey of community detection in complex networks using 22 23 23 nonnegative matrix factorization, *IEEE Transactions on Computational Social Systems* 9(2) (2021), 440–457.
- 24 24 [38] P.W. Holland, K.B. Laskey and S. Leinhardt, Stochastic blockmodels: First steps, *Social networks* 5(2) (1983), 109–137. 25 25 [39] R.F. i Cancho, C. Janssen and R.V. Solé, Topology of technology graphs: Small world patterns in electronic circuits,
- 26 26 [40] H. Jeong, B. Tombor, R. Albert, Z.N. Oltvai and A.-L. Barabási, The large-scale organization of metabolic networks, 27 27 *Nature* 407(6804) (2000), 651–654. *Physical Review E* 64(4) (2001), 046119.
- 28 28 [41] S.Y. Jeong, Y.S. Koh and G. Dobbie, Phishing detection on Twitter streams, in: *Trends and Applications in Knowledge* 29 29 *Discovery and Data Mining: PAKDD 2016 Workshops, BDM, MLSDA, PACC, WDMBF, Auckland, New Zealand, April 19, 2016, Revised Selected Papers 20*, Springer, 2016, pp. 141–153.
- 30 30 [42] D. Jin, Z. Yu, P. Jiao, S. Pan, D. He, J. Wu, P. Yu and W. Zhang, A survey of community detection approaches: From 31 31 statistical modeling to deep learning, *IEEE Transactions on Knowledge and Data Engineering* (2021).
- 32 32 [43] S. Kapoor,<https://www.sanjeevkapoor.com/> [accessed May 6, 2021]..
- 33 33 [44] L. Katzir and S.J. Hardiman, Estimating clustering coefficients and size of social networks via random walk, *ACM Transactions on the Web (TWEB)* 9(4) (2015), 1–20.
- ³⁴ [45] S. Khanna, C. Chattopadhyay and S. Kundu, INDoRI: Indian Dataset of Recipes and Ingredients and Its Ingredient³⁴ 35 35 Network, in: *International Conference on Complex Networks and Their Applications*, Springer, 2023, pp. 234–244.
- 36 36 [46] D. Knoke and S. Yang, Network fundamentals, *Social network analysis* 154 (2008), 3–14.
- ³⁷ 37 **of equal importance on actor-network theory by use of social network analysis,** *Contemporary Applications of Actor***³⁷** 38 38 *Network Theory* (2020), 211–230. [47] S. Kolli and D. Khajeheian, How actors of social networks affect differently on the others? Addressing the critique
- 39 39 [48] L. Laporta, J. Afonso and I. Mesquita, The need for weighting indirect connections between game variables: Social Net-40 40 work Analysis and eigenvector centrality applied to high-level men's volleyball, *International Journal of Performance Analysis in Sport* 18(6) (2018), 1067–1077.
- 41 41 [49] D.D. Lee and H.S. Seung, Learning the parts of objects by non-negative matrix factorization, *Nature* 401(6755) (1999), 42 788-791 42 788–791.
- 43 43 [50] R. Liu, S. Feng, R. Shi and W. Guo, Weighted graph clustering for community detection of large social networks, *Procedia Computer Science* 31 (2014), 85–94.
- 44
14 14 151] Y. Liu, A. Liu, X. Liu and X. Huang, A statistical approach to participant selection in location-based social networks for 45 45 offline event marketing, *Information Sciences* 480 (2019), 90–108.
- 46 46

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