***Cumulative Bayesian ridge for handling missing data***

Samih M. Mostafa a,\* Abdelrahman S. Mohamed a and Safwat Hamad b

aMathematics Department, Faculty of Science, South Valley University, Qena, Egypt

bFaculty of Computer and Information Sciences, Ain Shams University, Cairo, 11566, Egypt

\*samih\_montser@sci.svu.edu.eg

**Abstract.** Old approaches that manipulate missing values may lead to biased estimations. Besides, they may also decrease or magnify the statistical influence, which could result in unacceptable conclusions. The performance of various missing value imputation algorithms may depend on the amount of the missing values in the dataset and the dataset’s dimension. In this paper, the authors proposed a new algorithm for handling missing data against some registered practical imputation methods. The proposed algorithm depends on the Bayesian Ridge technique, which operates in a cumulative order with the aid of gain ratio feature selection to select the candidate feature to be imputed. The imputed feature will be included in the Bayesian Ridge equation to impute missing values in the next candidate feature. Here, the authors are attempting to choose the best imputation method succeeded to give high imputation accuracy with less imputation time. Finally, we applied the proposed algorithm on eight datasets with various missing values proportions generated from the missingness mechanisms. The empirical study indicates the effectiveness of the proposed algorithm with any missingness mechanism and with any missing data percentage.

**Keywords:** missing value, imputation, missingness mechanism, Bayesian Ridge and Gain ratio.

# Introduction

Avoiding missing data is the best approach for dealing with incomplete instances. All skilled researchers still encounter missing values that would happen for unpredictable reasons. In the data gathering stage, the researcher can make decisions about what data to collect and the way to screen data gathering. Both, the distribution, and scale of the features within the data, and the causes for missing data are two acute topics to select the right method for manipulating missing data[1].

Data preparation is considered the most significant and time-consuming task, which toughly impacts the success of the research. Feature selection lies in detecting a valuable subset of possible predictors from a large set of features. Refusing features with a large proportion of missing values (e.g., >50 %) is often a good rule of thumb. Nevertheless, it is not a risk-free route. Refusing a feature may lead to a loss of analytical power and capability to observe statistically significant differences, and it is often a cause of bias, affecting the representativeness of the outcomes. For these reasons, feature selection needs to be custom-made to the missing data mechanism. Imputation is often completed beforehand or later of feature selection[2].

## Handling missing data

For manipulating missing data, it is essential to know the reason for the missingness. This paper takes into consideration three general missingness mechanisms[2–5]:

* *Missing completely at random (MCAR):* If the likelihood of missingness is identical for all instances. The cause for the missingness in a feature X does not depend on X itself or any other feature within the dataset. In MCAR, missing value deletion does not bias your conclusions[6].
* *Missing at random (MAR):* If the likelihood of missingness is identical only within the detected data. The cause for the missingness in a feature X depends on other features within the dataset but does not depend on X itself. It is usually to model this process as a logistic regression, where the resulting feature equals 1 for detected cases and 0 for missing cases[6].
* *Missing not at random (MNAR):* If the likelihood of missingness for a feature X depends on X itself or other features that already include missing values[6].

The best approach for handling missing data is to avoid it through careful data gathering and follow up, along with determining missing data after the fact (for example, by detecting missing data or re-contacting study members). However, it is commonly impossible to avoid missing data in total; therefore, statistical methods for dealing with missing data are required. Since missing data are exceptionally complicated, statisticians cannot create a universal set of rules that manipulate all cases. So, they run emulation to detect the best method[7]. The approaches for handling missing data have to tailored to the causes of missingness, the dataset, and the percentage of missing data[2]. The best approach to manipulate that missing is to get rid of instances that involve missing values. In general, manipulating missing data using case deletion leads to accurate conclusions just for MCAR[8]. Imputation is the alternative approach for handling missing data and overwhelmed the disadvantages of the deletion approach[4].

The proposed algorithm depends on Bayesian ridge regression, so it is a regression model with a regularization parameter for the coefficients. The model satisfies the following[9]:

(1)

*Where*:

So follows a normal distribution characterized by variance and. and are regularizing parameters that follow gamma distribution. are hyper-parameters of the gamma prior distributions.

The structure of this paper as follows: Section 2 shows a literature review of manipulating the missing data, sections 3 and 4, present the proposed algorithm, and discuss the experimental implementation, respectively. Results and discussion described in 5. Finally, Section 6 concludes this paper.

# Literature review

For manipulating a dataset contains missing values. It is preferred to use deletion. A deletion might be complete deletion, list-wise deletion, or Complete Case Analysis, where all observations include one or more of their feature values missing are removed[4,10]. There might also be specific deletion, where only those observations canceled, which include more than a pre-specified percentage of their feature values that are missing[4,7,10,11]. There can also be pair-wise deletion or variable deletion, where the observations contain missing values in the features involved in the running analysis removed. In the worst case, each feature includes missing values through many instances that may cause the deletion of the whole dataset[12].

Imputation approaches benefit from all the information available within the dataset to predict the missing value, in which an applicable value is imputed instead of the missed value[10,11,13]. The imputed value might be median, mean, mode, or any pre-specified value of the feature that contains missing value[14–16], or might be acquired from case substitution. Imputed value can also be estimated using KNN(k nearest neighbors), regression models[3], cold deck imputation[17], EM (expectation-maximization) imputation[18–20], hot-deck imputation[21], etc. In techniques contain prediction models, a model is build based on available information within the dataset, then this model is used to predict values for the missing data[22]. Imputation methods used to deal with missing values if the missing values are of MCAR or MAR type, and if each record or feature in the dataset is important and a single observation does not include missing values across many features[12]. For MCAR type, missing values in a dataset manipulated using deletion, if could listwise deletion or maximum likelihood methods. There are not any general approaches to deal with MNAR missing values type[4,23]. Imputation types are single imputation or multiple imputation. In single imputation, a particular value is imputed rather than missing value[17]. Multiple imputation, where m full datasets acquired by imputing the missing values m times, the finale imputed dataset is the analysis average of these m datasets[24]. Although multiple imputation requires more resources[25], it has benefits over other methods, namely maximum likelihood techniques, single imputation, and deletion[26].

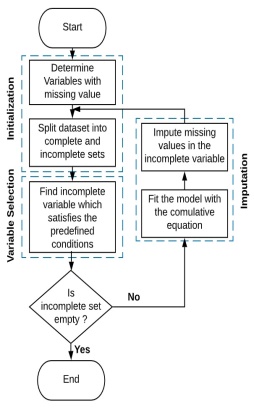
Single imputation approaches deal with all data values, even imputed ones as real values, which lead to inflated type I error as a result of not accounting uncertainty for a missing value. Inverse Probability Weighting (IPW) methods, which depend on the inverse of the detected probability to weight noted observations, in this way representing the entire data, even the missing values. Nevertheless, the imputation method produces more reliable performance[4,27]. Ordinary least squares (OLS), partial least squares (PLS), and singular value decomposition (SVD) are also good choices for multiple imputation[4]. For datasets having binary and ordinal features, Multi-Variate Normal Imputation (MVNI) and Fully Conditional Specification (FCS) approaches generate similar results and usually less biased. The model specification is granted easily by MVNI, but as a result, of its unrealistic nature, more or fewer people may have a problem with it. FCS tends to have a complex model specification as a result of requiring a single regression model for each feature whose missing values are going to be manipulated[28]. KNN is used by FINNIM (which is a practical nonparametric iterative multiple imputation approach) to predict missing values[29]. Sequential regression trees used as a Multiple imputation conditional model, which has the facility to detect complex relation and need slight correction by the user[30]. Handling missing values with predictive mean matching (PMM) approach is accomplished using a randomly drawn observation from a set of detected observations whose predictive mean is near to predictive mean of missing values[4]. Local residual draw (LRD) approach handles missing value using the predictive mean as in the situation of PMM, with extra randomly drawn from the residuals set of detected observations with predictive means near to that of the missing value[31]. Reinforcement programming (RP), which depends on Reinforcement Learning, gives better performance over mean per category imputation, zero imputation, and genetic algorithm (GA) in terms of the sum of square error and computational time[32]. Cumulative linear regression, which depends on the linear regression algorithm to handle missing data, works well for small and large datasets[3]. Manipulating missing values in features of concern with the aid of observed values from other features depends on the similarities of the instance values within the donor feature to deal with the missing values within the recipient feature. It works well when the proportion of the missing values is large[33].

# Proposed algorithm

Table 1 contains a list of terminologies that help in elaborating on the proposed algorithm. For any dataset, two cases may happen; the first case when all attributes include missing values, even the dependent attribute, and the second case when there is at least one perfect attribute. Suppose that the dependent attribute *y* does not involve any missing data and is the set of all independent attributes. The proposed algorithm splits the input dataset into two separate datasets and. The selection of the candidate attributes from to be imputed must exhibit the highest information gain ratio with the target attribute *y* using Eq. (4). The candidate attribute will be the dependent attribute and *y* and will be independent. The model fitted to impute the missing values in that attribute, and then the imputed attributewill be removed from and added to. Another attribute from will be selected to be the dependent attribute, and the model will be fit using, and, *y* as independent attributes. In the same way, another attribute will be select until be empty. The proposed algorithm presented in Figure 1, and Figure 2 shows the algorithm flow chart.

|  |
| --- |
| * ***Initialization***   + Identify features that contain missing values.     - ,and     - . * ***Feature* *selection***   + From , find select the feature with:     - Higher Gain Ratio () * ***Imputation***   + For each column in :     - Fit the model with cumulative Bayesian Ridge Regression equation:     ***Where****:*   * + - Impute missing values.   + Repeat until all missing values in all columns are imputed. |

**Figure 1.** Algorithm: CBRG (Cumulative Bayesian Ridge regression with Gain-ratio)



**Figure 2.** Algorithm flowchart

**Table 1.** List of terminologies

|  |  |  |
| --- | --- | --- |
| **Terms** | **Description** | **Comments** |
| n | number of all variables | Comp + Miss = n |
|  | set of complete variables |  |
|  | set of incomplete variables |  |
|  | imputed variable from X(Miss) |  |
| c | number of complete independents | c +m = n |
| m | number of variables contain missing values |  |
|  | set of missing observations in the dependent variable y |  |
|  | set of missing observations in the independent variable Xi |  |

# Experimental implementation

## Datasets

The authors perform an analysis of the effect of the proportion of missing values and dataset dimension on imputation time and the accuracy of such imputation. To accomplish this investigation, the authors used eight different datasets that usually studied in the literature (Table 2).

**Table 2.** Datasets specifications

|  |  |  |  |
| --- | --- | --- | --- |
| **Dataset name** | **Instances** | **Features** | **References** |
| graduate admissions | 500 | 8 | [34] |
| profit estimation of companies | 1000 | 6 | [35] |
| red & white wine dataset | 4898 | 12 | [36] |
| California | 20640 | 9 | [37] |
| diamonds | 53940 | 10 | [38] |
| BNG\_heart\_statlog | 1,000,000 | 14 | [39] |
| Poker Hand Dataset | 1,025,010 | 11 | [40] |
| diabetes | 442 | 11 | [41] |

The missing values generated from the three missingness mechanisms with different proportions 10%, 20%, 30%, and 40% missingness ratios for each type. Analysis for BNG\_heart\_statlog and Poker Hand datasets completed on randomly sampled sub-datasets of 10000, 15000, 20000, and 50000 of instances[4].

## Feature selection

Information gain's feature selection main disadvantage is that it is biased towards selecting features with lots of values, which encouraged Quinlan to define the Gain Ratio given by Eq. (4), which reduces this bias[42].

Where:

* *IG* is the information gain *X* is the set of examples.
* specifies the entropy, and *E* is the expected information of the attribute
* *n* is the number of possible values of attribute , and *IV* is the intrinsic value.
* is the Gain ratio.

In the feature selection stage, the proposed algorithm depends on selecting the feature that presents the most prominent information gain ratio with the target feature, the proposed algorithm named CBRG (Cumulative Bayesian Ridge regression with Gain-ratio).

## Performance evaluation

The performance of the proposed algorithm evaluated using RMSE, MAE, and R2, and time of imputation in seconds (t)[3].

*;*

Where and are the real and predicted values of the *lth* observation, respectively, and *n* is the number of samples.

# Results and discussion

If a method succeeded to give high imputation accuracy with less imputation time, and a small error, this method considered an efficient one.

This section subdivided into three subsections. The first subsection discusses the accuracy analysis, and the second explains the error analysis. The third discusses the imputation time.

## Accuracy analysis

The accuracy is known as how well the model in predicting the unknown data. The proposed algorithm selects and imputes the most appropriate feature; that offers higher information gain ratio with the output feature. The imputed feature will be included in the Bayesian ridge equation to impute the next candidate feature, until the imputation of all missing values within the dataset. Besides, the CBRG depends on the Bayesian Ridge, which in turn, is a probabilistic model with a ridge parameter. LeastSquares and Stochastic depend on the least-squares approach. LeastSquares impute the missing data via the best fit line from a set of predictors. Stochastic adds a random draw to the prediction from samples from the regression's error distribution. Norm constructs a Gaussian distribution from the sample mean besides variance of the detected data, and then random samples from this distribution are used to impute missing data.

The accuracy analysis represented by the evaluation of R2score given by Eq. (7), bigger value-is-better, on small size datasets, presented in Figure 3.b, Figure 4.b, Figure 5.b, and Figure 6.b. The performance of CBRG is better than Stochastic, Norm, Fast KNN, and Expectation-Maximization Imputation, and very close to Multivariate Imputation by Chained Equations (MICE). Also, the performance of CBRG is better or equals to the LeastSquares method. When imputing large size datasets, presented in Figure 7.b and Figure 8.b, the CBRG also performs well on large datasets.

The accuracy analysis for the BNG\_heart\_statlog dataset using random samples of 10000, 15000, 20000, and 50000 of instances, presented in Figure 9.b, Figure 10.b, Figure 11.b, and Figure 12.b, respectively. Also, the analysis for the Poker Hand dataset using random samples of 10000, 15000, 20000, and 50000 of instances, presented in Figure 13.b, Figure 14.b, Figure 15.b, and Figure 16.b, respectively. The performance of the CBRG on samples considered the best against stated methods; as a result of taking sample datasets, the data distribution becomes a normal distribution. As the CBRG depends on the Bayesian ridge technique, which in turn assumes that the independent features have a normal distribution, hence CBRG gives better accuracy.

## Error analysis

The MAE given by Eq. (6) will be smaller or equal to the RMSE given by Eq. (5), the more difference between them, the higher the variance in error in the sample. The errors are of the same magnitude only if MAE equals RMSE. For both RMSE and MAE, the lower value is better.

From Figure 3.a, and Figure 5.a, it observed that CBRG presented the smallest error, among other stated methods. In Figure 4.a, Figure 6.a, and Figure 7.a, it was remarked that CBRG granted lower error than Stochastic, Norm, Fast KNN, and Expectation-Maximization Imputation, but worse than LeastSquares and MICE. In Figure 8.a, it observed that CBRG presented smaller error than Norm, Fast KNN, and Expectation-Maximization Imputation, but worse than Stochastic, LeastSquares, and MICE. With increasing the size of the dataset, the CBRG presents a lower error.

The error analysis for the BNG\_heart\_statlog dataset using random samples presented in Figure 9.a, Figure 10.a, Figure 11.a, and Figure 12.a, the CBRG exhibited lower error than Stochastic, Norm, Fast KNN, and Expectation-Maximization Imputation and similar to LeastSquares and MICE in the provided error.

The error analysis for the Poker Hand dataset using random samples, presented in Figure 13.a, Figure 14.a, Figure 15.a, and Figure 16.a, the CBRG exhibited lower error than Stochastic, Norm, Fast KNN, and Expectation-Maximization Imputation and similar to LeastSquares and MICE in the provided error.

The CBRG assumes that the dependent feature and independent features have a normal distribution. Therefore, CBRG presents a lower error when manipulating sampled datasets.

## Imputation time

The selection of the candidate feature to be imputed by the CBRG depends on the feature selection technique of the information gain ratio. Calculating the information gain ratio depends on calculating the entropy, which is computationally expensive. However, CBRG exhibits a good imputation time with the generated samples, presented in Figure 9.a, Figure 10.a, Figure 11.a, and Figure 12.a for the BNG\_heart\_statlog dataset, and Figure 13.a, Figure 14.a, Figure 15.a, and Figure 16.a for the Poker Hand dataset. Also, when imputing too small size datasets, presented in Figure 3.a, and Figure 4.a, CBRG exhibits a good imputation time. The proposed algorithm takes long imputation time when manipulating large size datasets. The MICE is not efficient in imputation time. LeastSquares and Norm offer the best imputation time with all datasets. Fast KNN and EMI offer a good imputation time with small datasets but consume big imputation time when dealing with large datasets.

The results also revealed that the proposed method works well with any missingness mechanism and with any amount of missing data percentage.

(a) (b)

**Figure 3.** Comparison between the proposed method, LeastSquares, Stochastic, Norm, MICE, Fast KNN, and Expectation-Maximization Imputation (graduate admission dataset).

(a) (b)

**Figure 4**.Comparison between the proposed method, LeastSquares, Stochastic, Norm, MICE, Fast KNN, and Expectation-Maximization Imputation (diabetes dataset).

(a) (b)

**Figure 5**.Comparison between the proposed method, LeastSquares, Stochastic, Norm, MICE, Fast KNN, and Expectation-Maximization Imputation (Profit dataset).

(a) (b)

**Figure 6.** Comparison between the proposed method, LeastSquares, Stochastic, Norm, MICE, Fast KNN, and Expectation-Maximization Imputation (wine dataset).

(a) (b)

**Figure 7.** Comparison between the proposed method, LeastSquares, Stochastic, Norm, MICE, Fast KNN, and Expectation-Maximization Imputation (California dataset).

(a) (b)

**Figure 8.** Comparison between the proposed method, LeastSquares, Stochastic, Norm, MICE, Fast KNN, and Expectation-Maximization Imputation (diamond dataset).

(a) (b)

**Figure 9.** Comparison between the proposed method, LeastSquares, Stochastic, Norm, MICE, Fast KNN, and Expectation-Maximization Imputation (BNG (10000) dataset).

(a) (b)

**Figure 10.** Comparison between the proposed method, LeastSquares, Stochastic, Norm, MICE, Fast KNN, and Expectation-Maximization Imputation (BNG (15000) dataset).

(a) (b)

**Figure 11.** Comparison between the proposed method, LeastSquares, Stochastic, Norm, MICE, Fast KNN, and Expectation-Maximization Imputation (BNG (20000) dataset).

(a) (b)

**Figure 12.** Comparison between the proposed method, LeastSquares, Stochastic, Norm, MICE, Fast KNN, and Expectation-Maximization Imputation (BNG (50000) dataset).

(a) (b)

**Figure 13.** Comparison between the proposed method, LeastSquares, Stochastic, Norm, MICE, Fast KNN, and Expectation-Maximization Imputation (Poker (10000) dataset).

(a) (b)

**Figure 14.** Comparison between the proposed method, LeastSquares, Stochastic, Norm, MICE, Fast KNN, and Expectation-Maximization Imputation (Poker (15000) dataset).

(a) (b)

**Figure 15.** Comparison between the proposed method, LeastSquares, Stochastic, Norm, MICE, Fast KNN, and Expectation-Maximization Imputation (Poker (20000) dataset).

(a) (b)

**Figure 16.** Comparison between the proposed method, LeastSquares, Stochastic, Norm, MICE, Fast KNN, and Expectation-Maximization Imputation (Poker (50000) dataset).

# Conclusion

It is essential to handle missing data, as it happens in nearly all real-world research. Manipulating incomplete instances is very significant for observational analyses with several predictors.

In this paper, the authors studied a set of old published approaches used for manipulating missing data, reviewed their implementation on different datasets with different proportions of missing values generated from three missingness mechanisms. Besides, proposing a new algorithm, Cumulative Bayesian Ridge Regression, works in a cumulative order to impute all missing values in all attributes one after one. The candidate attribute is selected depending on the information gain ratio of feature selection. The proposed algorithm gives a better performance against the stated approaches. The proposed algorithm shows an acceptable running time and considered a fast method but not the fastest, as a result of calculating the gain ratio. The results also revealed that the proposed algorithm works well with any missingness mechanism and with any amount of missing data percentage. The CBRG, LeastSquares, and MICE present the best performance among other mentioned methods.

In future research, it is advisable to study the proposed imputation algorithm in additional datasets; additional units of standard error (like T-value and P-value) will be taken into mind when picking the candidate feature. The best future trend is to take the help of algorithms that deal with optimization problems with mixed features such as the GSA-GA algorithm[43].

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